



Prof. Dr. Andreas Podelski  
Dr. Matthias Heizmann  
Christian Schilling

Delivery: January 30th, 2017  
16:15 via the post boxes  
Discussion: February 1st, 2017

## Tutorial for Cyber-Physical Systems - Discrete Models

### Exercise Sheet 13

**Exercise 1: Positive normal form** 1 Point

Transform the following LTL formula into an equivalent LTL formula in PNF.

$$\neg\left(\left(\Box a\right) \rightarrow \left(\left(a \wedge \neg c\right) \cup \neg(\bigcirc b)\right)\right)$$

**Exercise 2: From LTL to NBA** 3 Points

Provide an NBA for each of the following LTL formulas:

(a)  $\Box(a \vee \neg \bigcirc b)$       (b)  $\Diamond a \vee \Box \Diamond(a \leftrightarrow b)$       (c)  $\bigcirc \bigcirc(a \vee \Diamond \Box b)$

You do not have to apply the algorithm from the lecture (which often produces large automata).

**Exercise 3: From LTL to GNBA using elementary sets** 3 Points

Consider the LTL formula  $\varphi := \neg a \cup a$  over the set of atomic propositions  $AP = \{a, b\}$ . Apply the algorithm from the lecture to obtain a GNBA  $\mathcal{G}_\varphi$  whose language is  $Words(\varphi)$  by executing the following steps.

- (a) Construct  $closure(\varphi)$ .
- (b) Construct the elementary sets w.r.t.  $closure(\varphi)$ .
- (c) Construct the GNBA  $\mathcal{G}_\varphi$ .